# Rainfall Estimation at S-44 Site 

(January $2^{\text {nd }}, 3^{\text {rd }}$, and $17^{\text {th }}, 1999$ Events)

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by

Alaa Ali \& Wossenu Abtew

Hydro Information Systems and Assessment Department
Environmental Monitoring and Assessment Division
South Florida Water Management District
3301 Gun Club Road
West Palm Beach, FL 33406

# RAINFALL ESTIMATION At S-44 SITE <br> (January $2^{\text {nd }}, 3^{\text {rd }}$, and $17^{\text {th }}, 1999$ events) 

Technical Notes

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## INTRODUCTION

The purpose of this communication is to reconstruct rainfall data at rain gage site S-44 (North Palm Beach) on the $2^{\text {nd }}$, the $3^{\text {rd }}$, and the $17^{\text {th }}$ of January of 1999 (unusually high rainfall events). The guge is believed to have malfunctioned on the $2^{\text {nc }}$ and $3^{\text {rd }}$ of January after recording a too high value, 32.53 inches. This value was revised later to 19.54 inches based on field comparison with a manual gage. Also, rainfall value recorded on the $17^{7 \mathrm{~h}}$ is believed to be too high ( 4.51 inches) compared to the surrounding gages and S-44 oufflow. Flow, rainfall, and groundwater level data measured at nearby stations have been used to estimate the questionable rainfall data at S -44. The estimation is performed by two independent methods; statistical data analysis and water budget computation. The two methods show consistent results. This document is divided into four sections: 1) Brief description of C-17 Basin, 2) Available data used for the estimation, 3) Statistical data analysis, and 4) Water budget computation.

## S-44 STATION AND THE C-17 BASIN

The C-17 basin is located in the northeastern part of Palm Beach County with an area of approximately 33 square miles (Figurel). The S-44 structure is located at Longitude and Latitude of $80^{\circ} 04^{\prime} 54^{\prime \prime} 26^{\circ} 49^{\prime} 00^{\prime \prime}$ respectively; and Easting and Northing of 955672 , and 903634 feet respectively. Rainfall is the only source of water supply to this basin while C - 17 is the only project canal. The C-17 canal and its only water control structure S-44 provide flood protection, drainage, and salt water intrusion prevention for the C-17 basin. Water flows Northward in the C-17 and is discharged to the Intracoastal Waterway through S-44 structure (Figure 1). For more information on C-17 basin, the reader is referred to the Eastern Palm Beach County Basin Atlas (Cooper and Lane, 1988).

## available data

Data used for this study are daily discharge flow at $\$$ - 44 structure and groundwater levels at nearby locations for the entire period of record. In addition, daily rainfall data at nearby stations including that at S-44 structure for the months of January/1999 were selected for the analysis. Information about these data is presented in Table 1. Data Locations are depicted in Figure 1. The use of these data to estimate rainfall at $\mathrm{S}-44$ site is presented in the remaining two sections.

Table 1. Information pertaining to the stations used for the estimation in this study.

| STATION | AGCY | TYPE | UNITS | !STAT | STRT | END | DBEEY | LAT | LONG | X, feet | Y. feet |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S44_R | WMD | Rain | Inches | SUM | 1991 | 1999 | 16674 | 264900 | 800454 | 955672 | 903634 |
| S44_S | WMD | FLOW | CFS | MEAN | 1985 | 1999 | 06795 | 264900 | \|800454 | 955672 | 903634 |
| PB-809_G | USGS | WELL | Ft, NGVD | MAX | 1975 | 1999 | 02669 | 264124 | 1800537 | 952104 | 857562 |
| PB-561_G | USGS | WELL | Ft., NGVD | MAX | 1973 | 1999 | 02694 | 264231 | 1801204 | 916959 | 864092 |
| PB-109_G | USGS | WELL | Ft., NGVD | MAX | 1950 | 1992 | 02785 | 264842 | 801148 | 918173 | 901562 |
| JUPITER_R | WMD | RAlN | Inches | SUM | 1976 | 1998 | 05888 | 265623 | 800603 | 949103 | 94832 |
| PLANT IN_R | WPBC | Rain | Inches | SUM | 1944 | 1999 | 05966 | 264254 | 80034 | 96228 | 86 |
| SIRG | WMD | RAIN | Inches | SUM | 1994 | 1999 | 15730 | 265426 | 801130 | 919583 | 936308 |
| $\mathrm{ClSW}_{\text {R }}$ | WMD | Rain | Inches | SUM | 1992 | 1999 | 16603 | 265219 | 801442 | 902277 | 923377 |
| WPB AIRP_R | WMD | RAIN | Inches | SUM | 1991 | 1999 | 16610 | 264041 | 800635 | 946873 | 85.3183 |
| S46_R | WMD | RAIN | Inches | SUM | 1993 | 1999 | 16673 | 265603 | 800830 | 935812 | 946210 |
| WPBFS_R | WMD | RAIN | Inches | SUM | 1997 | 1999 | GA832 | 264122 | 801105 | 922335 | 857199 |
| Haverhill 8 Eamest | $\begin{aligned} & \text { WPB.W. } \\ & \text { W.T.P } \end{aligned}$ | RAIN | Inches | SUM | 1999 | 1999 | N/A | 264424 | 800706 | 943963 | 875619 |



Figure 1. C17 Basin and the nearby stations used for this analysis.

## STATISTICAL ANALYSIS

In this section, rainfall at $\$-44$ is expressed in-terms-of:

1) Nearby rainfall data using the Reciprocal Square Distance Interpolation (RSDI),
2) Flow data at S-44 using correlation and regression analysis, and
3) Nearby Groundwater level data using correlation and regression analysis.

The purpose of this exercise is to:

1) Investigate the applicability of each method in providing consistent rainfall estimation with the hydrologic conditions reported on these days;
2) Provide a useful check if any other source offinformation is made available eserrar data);
3) Benerit the subsequent water budgct computation.

## Rainfall estimation using neighbor stations.

The average distance between $\mathrm{S}-44$ and the nearest eight stations is about 9.3 miles with the reareat station (PLANT IN) located 7 mitecto the southeast. Given the nature of such a local rainfall stom; these stations are not near enough to provide a cealistic representation for this storm. Using the Reciprocal Square Distance Interpolation, RSDI, Method (Tabios and Salas, - 1985, Abtew et. al., 1993), and the nearest eight rainfall stations, the estimated rainfall on the $2^{\text {nd }}$, the $3^{\text {rd }}$, and $17^{\text {th }}$ of January of 1999 are: $4.6,1.5$, and 1.8 inches. The estimates on the $2^{\text {nd }}$ and $3^{\text {rd }}$ are not consistent with other sources of information such as reported flooding, radar data, and flow discharge at S-44 structure. However, the January $/ 17^{\text {th }}$ estimate is consistent with that based on the Rainfall-Flow analysis. It was concluded that the January $2^{\text {nd }}$ and $3^{\text {rd }}$ events at $\mathrm{S}-44$ can not be estimated using the surrounding rain gages. .- --- -- .

## Rainfall-Flow Correlation and Regression

Correlation and linear regression analysis was conducted between S-44 daily rainfall (inches) and daily flow (cfs) data for several minimum rainfall "cut-off" values. Table 2 shows the results of this analysis. Rainfall data with minimum cut-off value of 1.0 -inch shows the highest corelation (0.75). Table 3 shows the regression coefficients, the observed flow and the estimated rainfall on the $2^{\text {nd }}, 3^{\text {rd }}$, and $17^{\text {th }}$ of January of 1999 .

Table 2. S-44 Rainfall-Flow Corrclation and Regression results.

| cut-off <br> (inches) | Cortelation | Lag <br> (days) | Number of <br> observations | Regression |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0.5 | 0.724 | 0 | 296 | 0 | 0.25 |
| 1.0 | 0.749 | 0 | 134 | 0.49 | 0.00471 |
| 1.5 | 0.749 | 0 | 65 | 0.70 | 0.00521 |
| 2.0 | 0.704 | 0 | 42 | 0.79 | 0.00509 |

Table 3. Observed flow and estimated rainfall at $S-44$ based on Rainfall-Flow Analysis.

| Date | Flow <br> (CFS) | Rainfall <br> (inches) | NOTES |
| :--- | :--- | :--- | :--- |
| $01 / 02 / 99$ | 1902.5 | 10.12 | Rainfall (inches) $=0.49+0.00506 *$ Flow (cfs) <br> Regression coefficients are estimated based on 1 inch <br> $01 / 03 / 99$ |
| 1132.96 | 6.22 | Rinimum rainfall cut-off value, and 134 data points. |  |
| $01 / 17 / 99$ | 267.23 | 1.85 |  |

## Rainfall-Groundwater level Correlation

Three groundwater level stations (PB-809_G, PB-561_G, and PB-109_G) were used for this analysis. The distance of these stations to $S-44$ are $8.75,10.50$, and 7.11 miles respectively. A Correlation analysis betwcen a threc-day moving sum of $\mathrm{S}-44$ rainfall and the corresponding water level change within this window shows that station PB-109_G is highly correlated with S44 rainfall data while the other two stations are poorly correlated. Table 4 presents the correlation and regression analysis results for "PB-109_G" for several minimum cut-off values of three-day rainfall.

Table 4. Rainfall-Groundwater level Contelation and Regression results.

| cut-off <br> (inches) | Cortelation | $\begin{aligned} & \hline \text { Lag } \\ & \text { (days) } \end{aligned}$ | Number of observations | Regression |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | a | b |
| 1.0 | 0.83 | 0 | 63 | 1.04 | 6.89 |
| 1.5 | 0.89 | 0 | 31 | 1.39 | 7.11 |
| 2.0 | 0.92 | 0 | 15 | 1.69 | 7.05 |
| 2.5 | 0.93 | 0 | 10 | 1.84 | 6.97 |

Table 4 indicates a robust correlation structure between water levels at station "PB109 G" and three-day rainfall sum at S-44. Unfortunately, water level data are not available beyond May/1992 at this station. Therefore, a direct estimation of rainfall using the PB-109_G station is not possible. However, this rainfall-water level relationship is useful for the water budget computation. Based on 1 -inch minimum rainfall cut-off value, this relationship is given as follows:
where:

$$
\rho_{1}=1.04+6.89^{*} \Delta w_{t}
$$

$\rho_{\mathrm{t}}=$ rainfall sum, in inches, in a three-day period up to " t " day. $\Delta \mathrm{w}_{\mathrm{l}}=$ Water level change, in feet, within the same period.

## WATER BUDGET ANALYSIS

As mentioned earlier, rainfall is the only source of water supply to the C 17 basin. Based on S-44 daily flow data (Figure 2), it is noticed that the January $2^{\text {nd }}$ storm effect on the S-44 flow lasts up to the $15^{\text {th }}$ of January. Therefore, the water budget analysis was considered for the period between the $2^{\text {nd }}$ to the $15^{\text {th }}$ of January ( 14 days) within the $\mathrm{C}-17$ basin. The water budget components are:


Figure 2. S-44 Outflow during January.

## Rainfall

Rainfall accumulated over the period of January $5^{\text {th }}$ to the $15^{\text {th }}$ was 0.71 inch.
Rainfall accumulated over the budget period $=$ rainfall of January $(2,3$, and 4$)+0.71$

$$
=\rho_{4}+0.71
$$

## Evapotranspiration (ET)

Based on evapotranspiration study at the Everglades Nutrient Removal Project (Abtew, 1996), January daily ET is 0.1 inch. Therefore, the ET over the budget period is estimated as:

$$
\mathrm{ET}=0.1 * 14=1.4 \text { inches. }
$$

## S-44 outflow

S-44 discharge volume $=12075 \mathrm{ac}$-ft.,
equivalent depth in inches = discharge volume/(total area in acre)*12

$$
=12075 /(33 * 640)^{*} 12=6.86 \text { inches. }
$$

## Change in storage

$$
\begin{aligned}
\delta & =\Delta w_{t} * 12 * n_{\mathrm{e}} \\
& =\left(\rho_{\mathrm{t}}-1.04\right) / 6.89 * 12^{*} \mathrm{n}_{e} \text {, where: }
\end{aligned}
$$

$\rho_{\mathrm{l}}=$ rainfall sum in a three-day period up to " t " day.
$\delta=$ Change in subsurface storage in inches.
$\pi_{c}=$ Effective porosity; dominant soil type is Basinger and Myakka fine sand. An average value for the effective porosity for sandy soils is 0.32 inch (Marsily, 1986).

## Water Budget Computation

The general mass balance equation is:
IN-OUT $=$ Change in the storage.
Where:
IN = Rainfall depth accumulated during this period;
OUT = Evapotranspiration, and equivalent depth due to S-44 outflow;
Change in storage $=$ Depth of water causing volume change in surface and subsurface storage.

Given the above components, effective porosity of 0.32 , and assuming no significant change in surface storage between the beginning and end of the water budget analysis period;
$\rho_{4}+0.71-(1.4+6.86)=\delta=\left(\rho_{4}-1.04\right) / 6.89 * 12 * n_{e}$
$0.44 * \rho_{4}=6.97$
$\rho_{4}=15.84$ inches.
Since rainfall on January $/ 4^{\text {th }}$ is 0 ; the rainfall sum for the $2^{\text {nd }}$ and the $3^{\text {rd }}$ of January is 15.84 inches.

Based on the rain-flow computation, rainfall on the $2^{\text {nd }}$ and $3^{\text {rd }}$ is 10.13 and 6.23 inches respectively. Using the same proportions; rainfall, based on water level correlation, is 9.81 and 6.03 inches on the $2^{\text {nd }}$; and $3^{\text {rd }}$ respectively.

## CONCLUSION

In this study, the estimation of questionable rainfall data at S-44 was carried out using statistical and water budget analyses. In the statistical data analysis, three sources of data were used (nearby rainfall data, S-44 flow data, and nearby groundwater level data). Estimation provided by the RSDI method using rainfall data from surrounding gages is inconsistent with the hydrologic conditions and radar data reported in that area on January $2^{\text {nd }}$ and $3^{\text {rd }}$. However, such an estimate on the $17^{\text {th }}$ is consistent with that estimated by the rainfall-flow analysis. The rainfall-flow analysis and the water budget analysis provided consistent estimates. Using the available information and the results of these analyses, average estimated rainfall on January $2^{\text {id }}$, $3^{\text {rd }}$, and $17^{\text {th }}$ are 10,6 , and 1.8 inches respectively.

## REFERENCES

Abtew, W. Evapotranspiration Measurements and Modeling for Three Wetland Systems in South Florida. American Water Resources Association, Vol. 32, No. 3, June 1996.

Abtew, W., J. Obeysekera, and G. Shih. 1993. Spatial analysis for monthly rainfall in South Florida. Water Resources Bulletin, 29(2): 179-188, 1993.

Cooper, R, and J. Lane, 1988. An Atlas of Eastern Palm Beach County Surface Water Management Basins. Technical Memorandum, Water Resources Division, Resource Planting Department, South Florida Water Management District.

Marsily, G. 1986. Groundwater Hydrology for Engineers. Harcourt Brace Jovanovich, Publishers, Academic Press, $\mathrm{INC}_{6}, 440 \mathrm{p}$.

Tabios III, G. and J. Salas. 1985. A comparative analysis of techniques for spatial interpolation of precipitation. Water Resources Bulletin, 21 (3): 365-380.

